## HW 9_Ch6

Q1) For the periodic signals $x(t)$ and $y(t)$ shown below:

a) Find the exponential Fourier series for $x(t)$ and $y(t)$.
b) Sketch the amplitude and phase spectra for signal $x(t)$.
c) Use Parseval's theorem to approximate the power of the periodic signal $x(t)$ by calculating the power of the first $N^{\mathrm{th}}$ harmonics, such that the strength of the $N^{\mathrm{th}}$ harmonic is $10 \%$ or more of the power of the DC component.

Q2) The exponential Fourier series of a certain function is given as

$$
x(t)=(2+j 2) \mathrm{e}^{-j 3 t}+j 2 \mathrm{e}^{-j t}+3-j 2 \mathrm{e}^{j t}+(2-j 2) \mathrm{e}^{j 3 t}
$$

a) Sketch the exponential Fourier spectra.
b) By inspection of the spectra in part (a), sketch the trigonometric Fourier spectra for $x(t)$. Find the compact trigonometric Fourier series from these spectra.
c) Show that the trigonometric series found in part (b) is equivalent to the exponential series for $x(t)$.
d) Find the signal bandwidth.

Q3) Figure below shows the exponential Fourier spectra of a periodic signal $x(t)$.
a) By inspection of the Figure find the exponential Fourier series representing $x(t)$.
b) By inspection of the Figure, sketch the trigonometric Fourier spectra for $x(t)$.
c) By inspection of the trigonometric Fourier spectra found in part (b), find the trigonometric Fourier series for $x(t)$.
d) Show that the series found in parts (a) and (c) are equivalent.


Q4)Find the response of an LTIC system with transfer function $H(s)=\frac{s}{s^{2}+2 s+3}$ to the periodic input

$$
x(t)=(2+j 2) \mathrm{e}^{-j 3 t}+j 2 \mathrm{e}^{-j t}+3-j 2 \mathrm{e}^{j t}+(2-j 2) \mathrm{e}^{j 3 t}
$$

Q5) Find the exponential Fourier series for a periodic signal $x(t)$ shown in Figure below


The signal $x(t)$ is applied at the input of an LTIC system shown above. Find the expression for the output $y(t)$.

